

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER		CANDIDATE NUMBER			
MATHEMATICS		0580/04, 0581/04			
Paper 4 (Extended)	May/June 2009			
		2 hours 30 minutes			
Candidates answer	on the question paper.				
Additional Materials	s: Electronic calculator Mathematical tables (optional)	Geometrical instruments Tracing paper (optional)			
READ THESE INS	TRUCTIONS FIRST				

Write your Centre number, candidate number and name on all the work you hand in. Write in dark blue or black pen. You may use a soft pencil for any diagrams or graphs. Do not use staples, paper clips, highlighters, glue or correction fluid. DO **NOT** WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures.

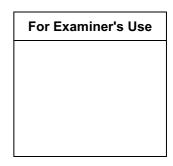
Give answers in degrees to one decimal place.

For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 130.



This document consists of **19** printed pages and **1** blank page.



2 A normal die, numbered 1 to 6, is rolled 50 times.

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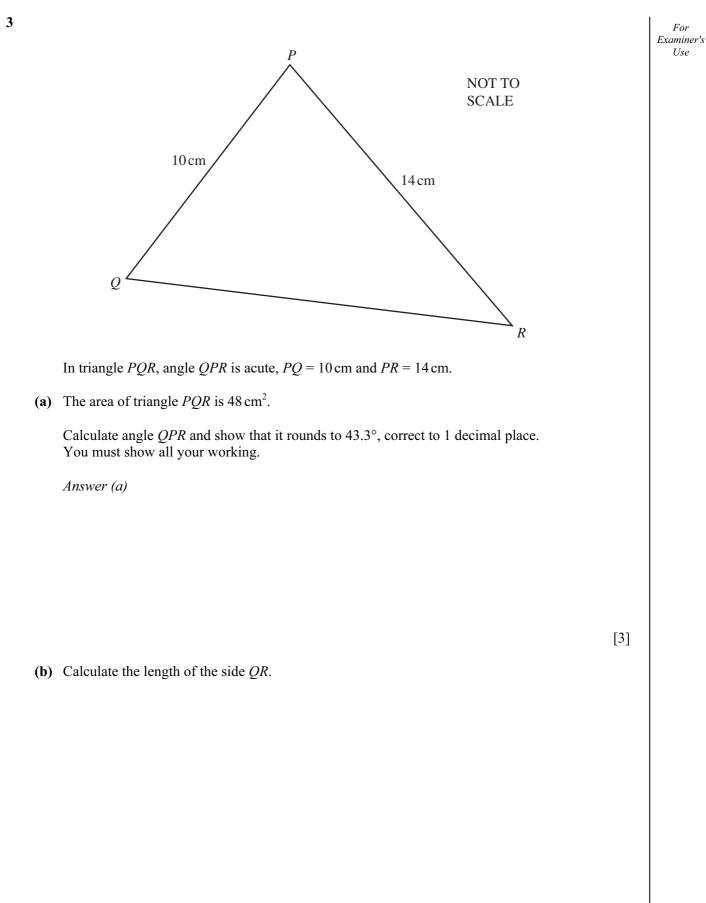
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[1]

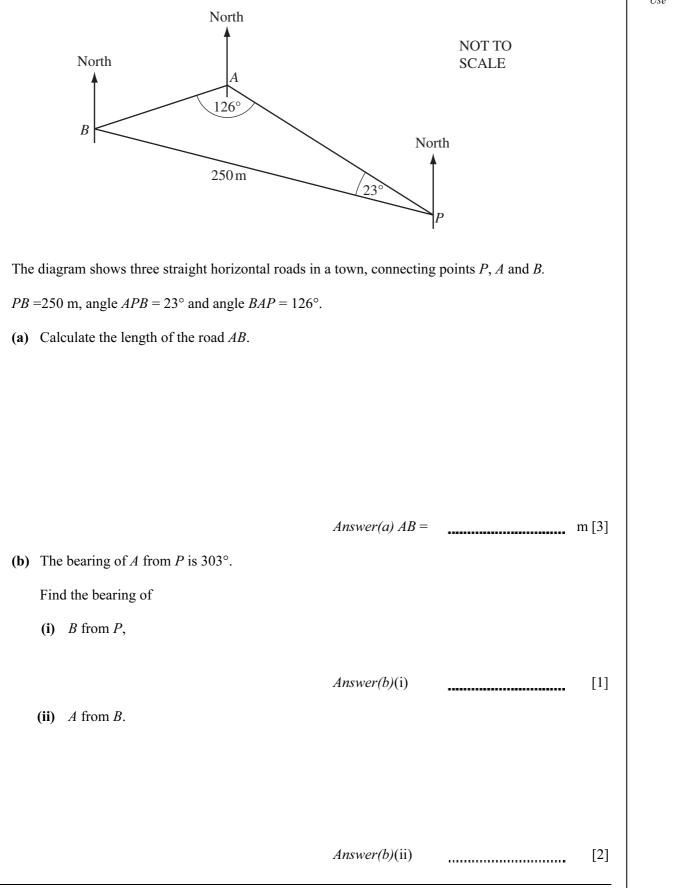
[2]

The results are shown in the frequency table. 1 2 3 4 Score 5 6 Frequency 15 10 7 5 6 7 (a) Write down the modal score. Answer(a) (b) Find the median score. Answer(b) (c) Calculate the mean score. Answer(c) (d) The die is then rolled another 10 times. The mean score for the 60 rolls is 2.95. Calculate the mean score for the extra 10 rolls. Answer(d)

[3]



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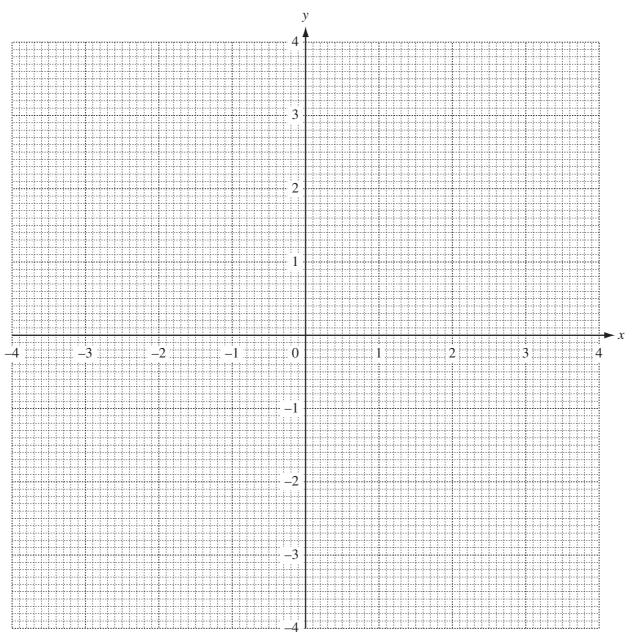
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5 (a) The table shows some values for the equation $y = \frac{x}{2} - \frac{2}{x}$ for $-4 \le x \le -0.5$ and $0.5 \le x \le 4$.

x	-4	-3	-2	-1.5	-1	-0.5	0.5	1	1.5	2	3	4
У	-1.5	-0.83	0	0.58			-3.75		-0.58	0	0.83	1.5

(i) Write the missing values of y in the empty spaces.

(ii) On the grid, draw the graph of
$$y = \frac{x}{2} - \frac{2}{x}$$
 for $-4 \le x \le -0.5$ and $0.5 \le x \le 4$.



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[5]

(b) Use your graph to solve the equation $\frac{x}{2} - \frac{2}{x} = 1$. Answer(b) x = or x =

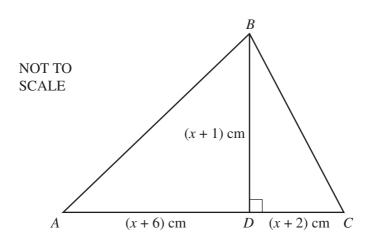
(c) (i) By drawing a tangent, work out the gradient of the graph where x = 2.

Answer(c)(i) [3] (ii) Write down the gradient of the graph where x = -2. Answer(c)(ii) [1] (d) (i) On the grid, draw the line y = -x for $-4 \le x \le 4$. [1] (ii) Use your graphs to solve the equation $\frac{x}{2} - \frac{2}{x} = -x$. Answer(d)(ii) x = or x =[2] (e) Write down the equation of a straight line which passes through the origin and does not intersect the graph of $y = \frac{x}{2} - \frac{2}{x}$.

> Answer(e) [2]

[2]

6 (a)



In triangle ABC, the line BD is perpendicular to AC.

AD = (x + 6) cm, DC = (x + 2) cm and the height BD = (x + 1) cm.

The area of triangle ABC is 40 cm^2 .

(i) Show that $x^2 + 5x - 36 = 0$.

Answer (a)(i)

(ii) Solve the equation $x^2 + 5x - 36 = 0$.

(iii) Calculate the length of *BC*. $Answer(a)(ii) x = \dots \text{ or } x = \dots \text{ [2]}$ $Answer(a)(iii) BC = \dots \text{ cm [2]}$

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[3]

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- (b) Amira takes 9 hours 25 minutes to complete a long walk.
 - (i) Show that the time of 9 hours 25 minutes can be written as $\frac{113}{12}$ hours.

Answer (b)(i)

[1]

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(ii) She walks (3y + 2) kilometres at 3 km/h and then a further (y + 4) kilometres at 2 km/h.

Show that the total time taken is $\frac{9y+16}{6}$ hours. Answer(b)(ii)

[2]

(iii) Solve the equation
$$\frac{9y+16}{6} = \frac{113}{12}$$
.

Answer(b)(iii) y =[2]

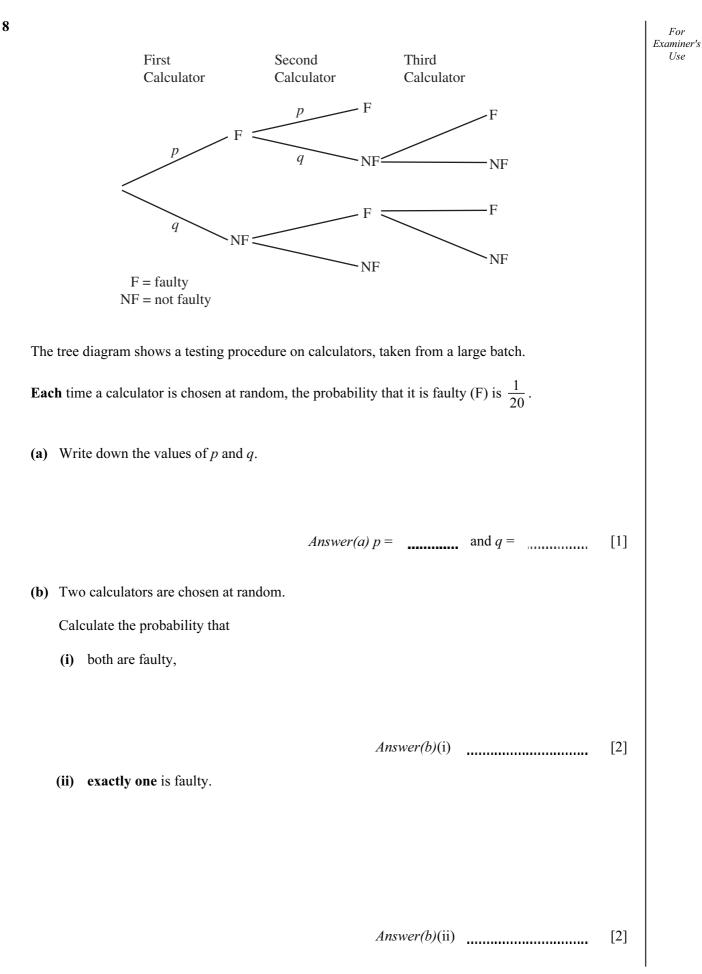
(iv) Calculate Amira's average speed, in kilometres per hour, for the whole walk.

Answer(b)(iv) km/h [3]

(d) One metal bar, of volume 4840 cm^3 , is melted down to make 4200 identical small spheres. For Examiner's UseAll the metal is used. (i) Calculate the radius of each sphere. Show that your answer rounds to 0.65 cm, correct to 2 decimal places. [The volume, V, of a sphere, radius r, is given by $V = \frac{4}{3}\pi r^3$.] Answer(d)(i) [4] (ii) Calculate the surface area of each sphere, using 0.65 cm for the radius. [The surface area, A, of a sphere, radius r, is given by $A = 4\pi r^2$.] *Answer(d)*(ii) _____ cm² [1] (iii) Calculate the total surface area of all 4200 spheres as a percentage of the surface area of the metal bar. Answer(d)(iii) % [4]

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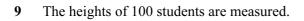
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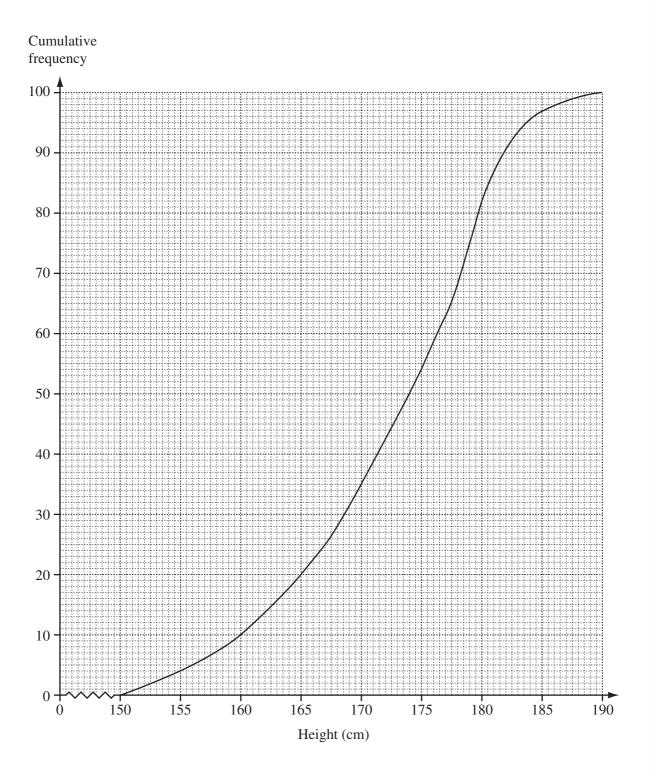
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(c) If exactly one out of two calculators tested is faulty, then a third calculator is chosen at random. Calculate the probability that exactly one of the first two calculators is faulty and the third one is faulty. Answer(c) [2] (d) The whole batch of calculators is rejected either if the first two chosen are both faulty or if a third one needs to be chosen and it is faulty. Calculate the probability that the whole batch is rejected. Answer(d) [2] (e) In one month, 1000 batches of calculators are tested in this way. How many batches are expected to be rejected? Answer(e) [1]

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The results have been used to draw this cumulative frequency diagram.



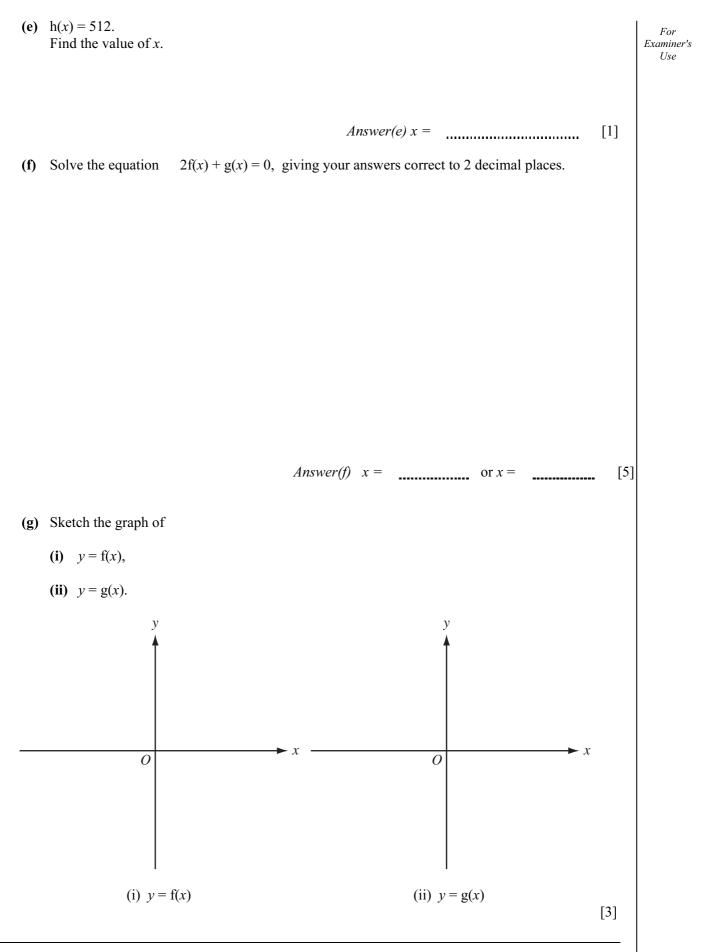
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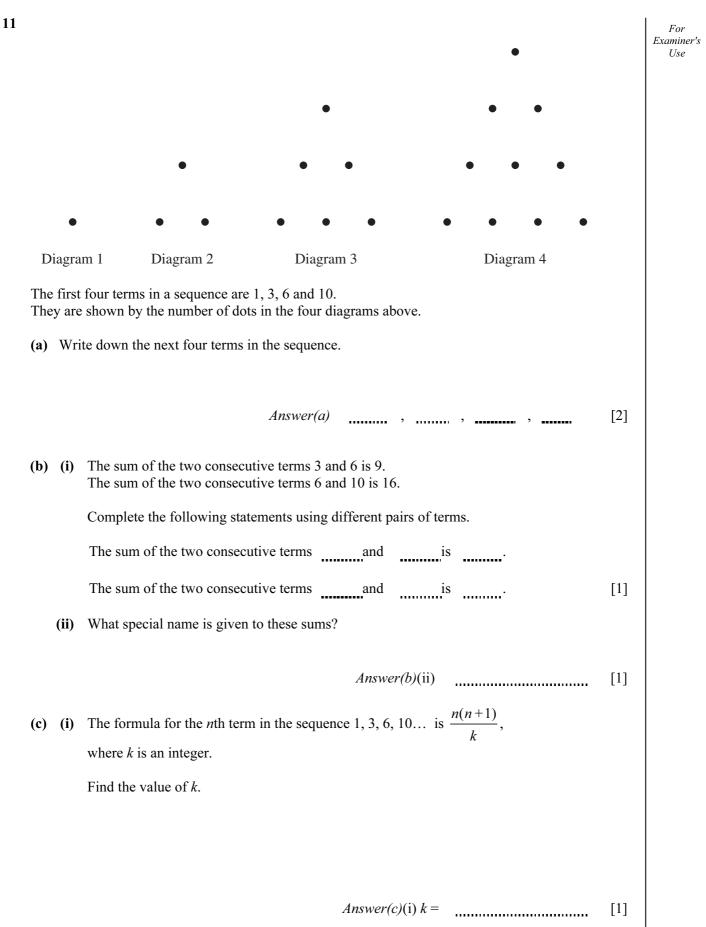
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(a)	F								For Examiner's
	(i	i)	the median he	ight,				543	Use
	(ii	i)	the lower quar	rtile,	An.	<i>swer(a)</i> (i)		cm [1]	
	,				An	swer(a)(ii)		cm [1]	
	(iii	i)	the inter-quart	tile range,					
	(iv	r)	the number of	f students with a her		<i>swer(a)</i> (iii)		cm [1]	
						swer(a)(iv)		[2]	
(b)	T	he	frequency tabl	le shows the inform	nation about the 10	0 students who v	vere measured.		
		Н	eight (<i>h</i> cm)	$150 < h \le 160$	$160 < h \le 170$	$170 < h \le 180$	$180 < h \le 19$	90	
			Frequency			47	18		
	(i (ii			lative frequency dia				[1]	
	(11	9				students.			

Answer(b)(ii) cm [4]

10	$\mathbf{f}(x) = 2x - 1$	$g(x) = x^2 + 1$ $h(x) =$	$=2^{x}$	For Examiner's Use
	(a) Find the value of			
	(i) $f(-\frac{1}{2})$,			
	(ii) $g(-5)$,	Answer(a)(i)		[1]
		Answer(a)(ii)		[1]
	(iii) h(-3).			
		Answer(a)(iii)		[1]
	b) Find the inverse function $f^{-1}(x)$).		
		Answer(b) $f^{-1}(x) =$		[2]
	(c) $g(x) = z$. Find x in terms of z.			
		Answer(c) x =		[2]
	(d) Find $gf(x)$, in its simplest form.			
		Answer(d) $gf(x) =$		[2]





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